

A black and white photograph of Albert Einstein. He is shown from the chest up, wearing a dark sweater over a collared shirt. He has his characteristic wild hair and a prominent mustache. He is looking slightly to his left with a thoughtful expression. His right hand is raised, holding a piece of chalk, and he appears to be writing on a chalkboard. The chalkboard behind him is partially visible, showing some mathematical notation and diagrams, including what looks like the equation  $R_i = 0$ .

## Hypercritical accretion onto neutron stars and the induced gravitational collapse paradigm of gamma-ray bursts associated with supernovae

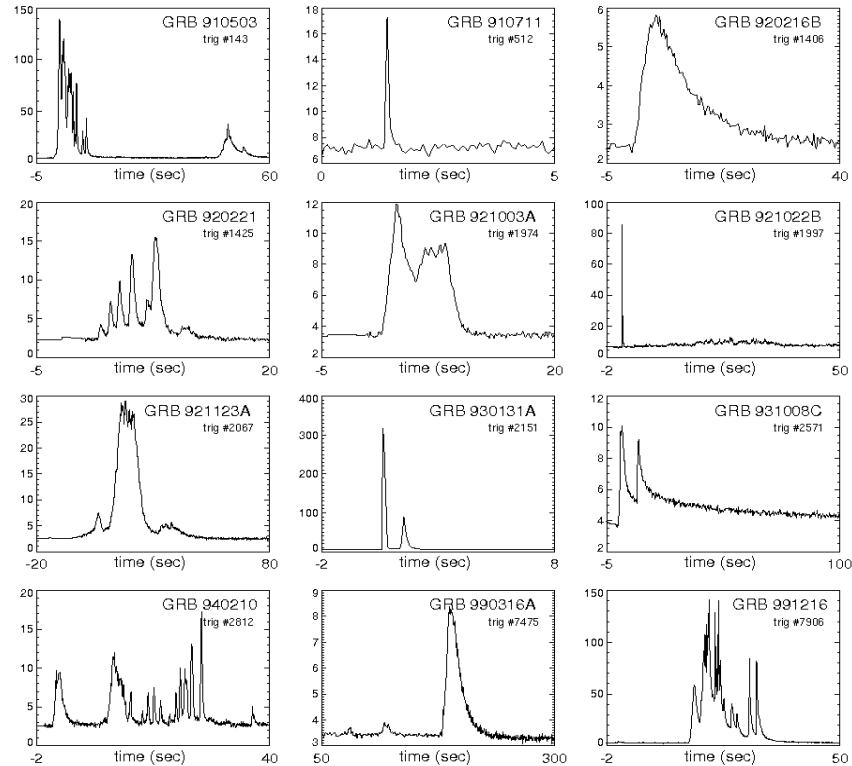
Jorge Armando Rueda Hernández – ICRA-Net and Sapienza University of Rome

The 1<sup>st</sup> Sandoval Vallarta Meeting on Relativistic Astrophysics, 30 November-4 December, Mexico City, Mexico  
2015

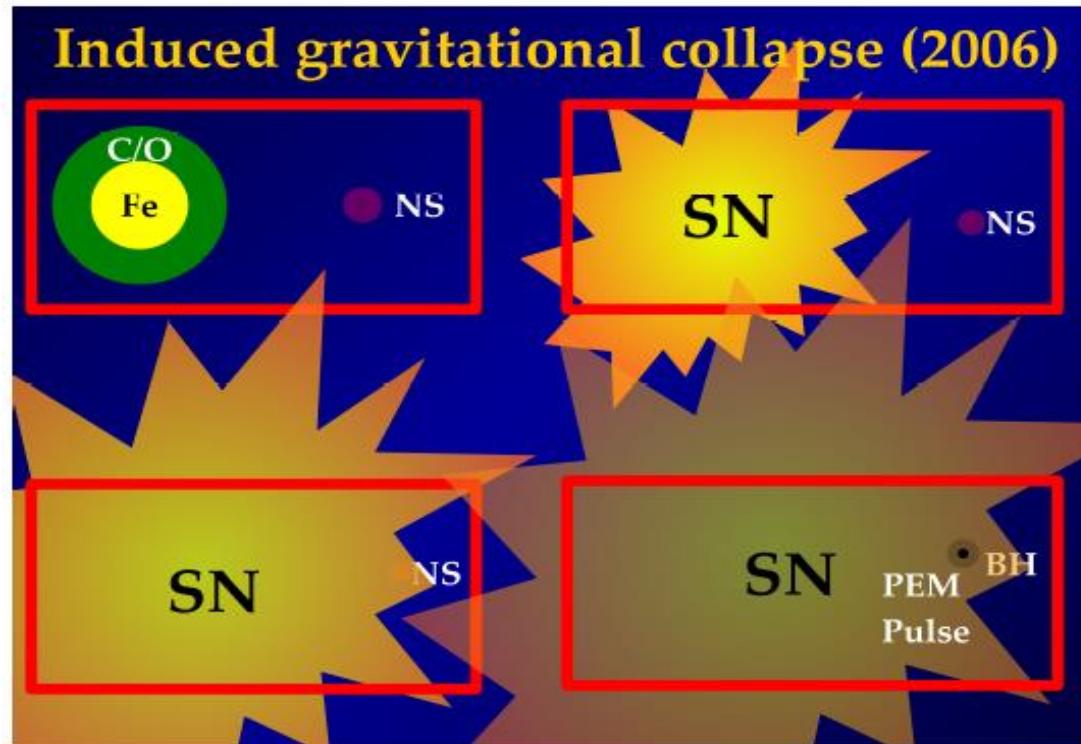


# Gamma-Ray Bursts

- GRBs are cosmological explosions (observed up to  $z=9.4$  GRB 090429B)
- Most energetic objects (up to a few  $10^{54}$  erg of isotropic energy)
- Complex light-curves but in general characterized by a prompt and an extended afterglow emission
- Duration: “Short” GRBs <2 seconds and “Long” GRBs >2 seconds
- Probe the Physics of *Gravitational Collapse and Black Hole formation*

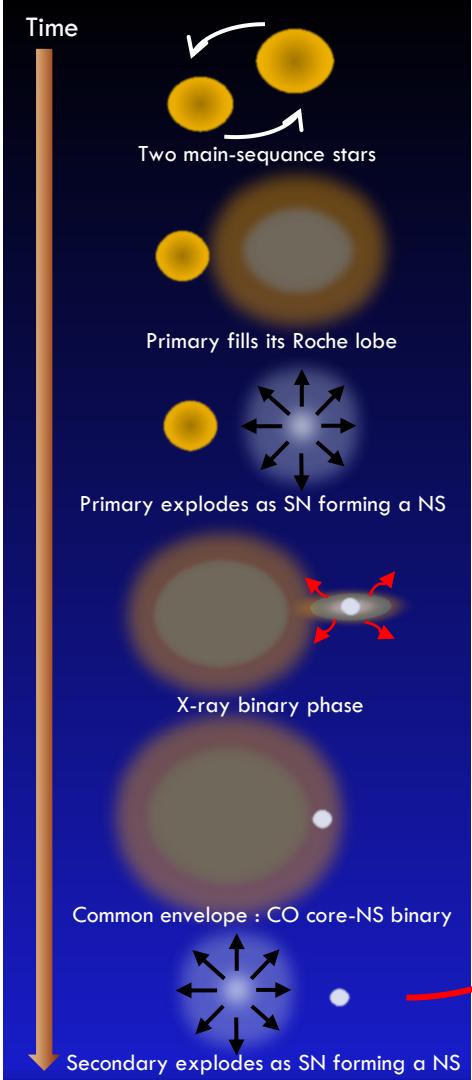


# Induced Gravitational Collapse (IGC) Paradigm



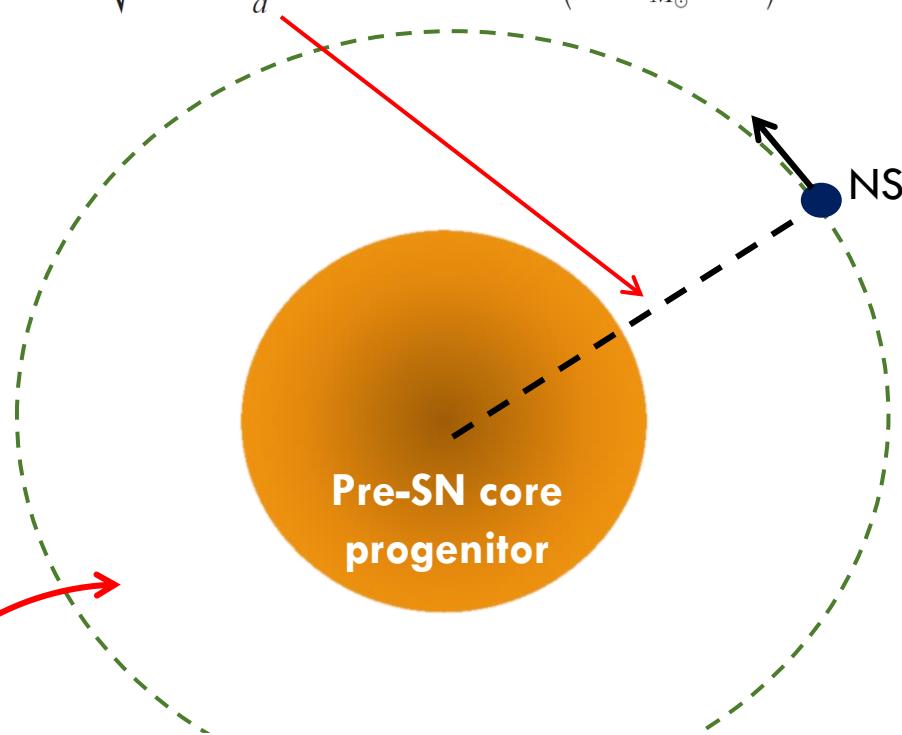
Ruffini et al. MG11-Berlin (2006)

Nomoto et al.  
1994  
Iwamoto et al.  
1994  
Nomoto et al.  
1995



# The Induced Gravitational Collapse

$$v_{\text{orb}} = \sqrt{\frac{G(M_{\text{SN-prog}} + M_{\text{NS}})}{a}} = 1.15 \times 10^8 \left( \frac{M_{\text{SN-prog}} + M_{\text{NS}}}{M_{\odot}} \right)^{1/2} \text{ cm s}^{-1}$$



$$P = \sqrt{\frac{4\pi^2 a^3}{G(M_{\text{SN-prog}} + M_{\text{NS}})}} = 545 \left( \frac{M_{\text{SN-prog}} + M_{\text{NS}}}{M_{\odot}} \right)^{-1/2} \text{ s}$$

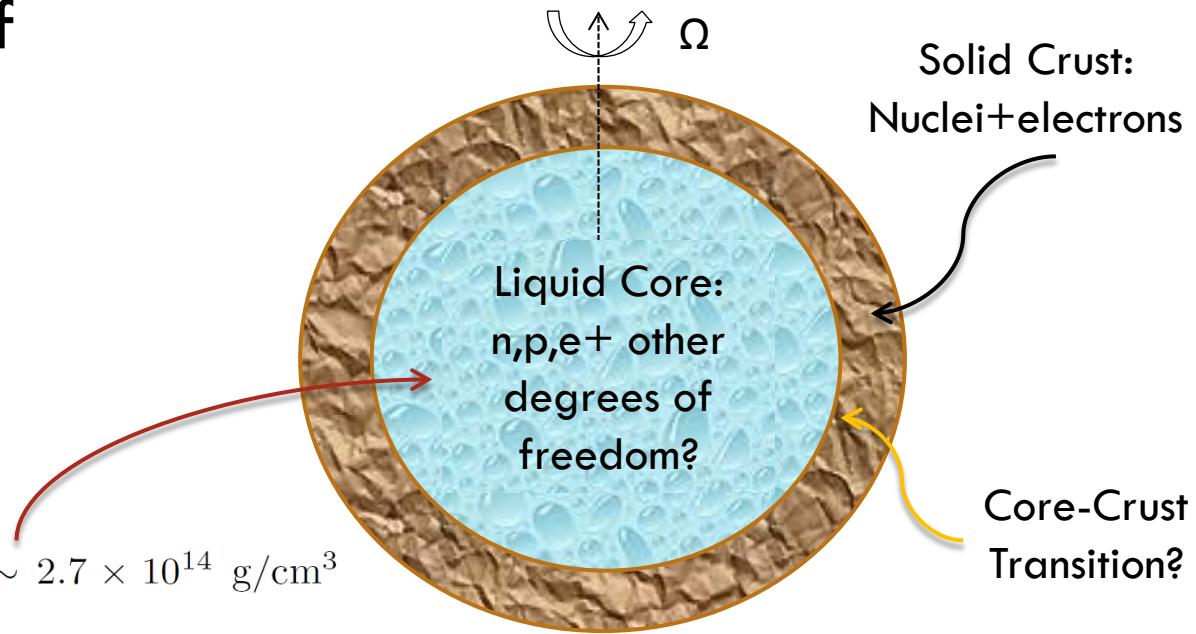
# Oppenheimer & Volkoff (1939) versus Today Neutron Stars

## Oppenheimer-Volkoff

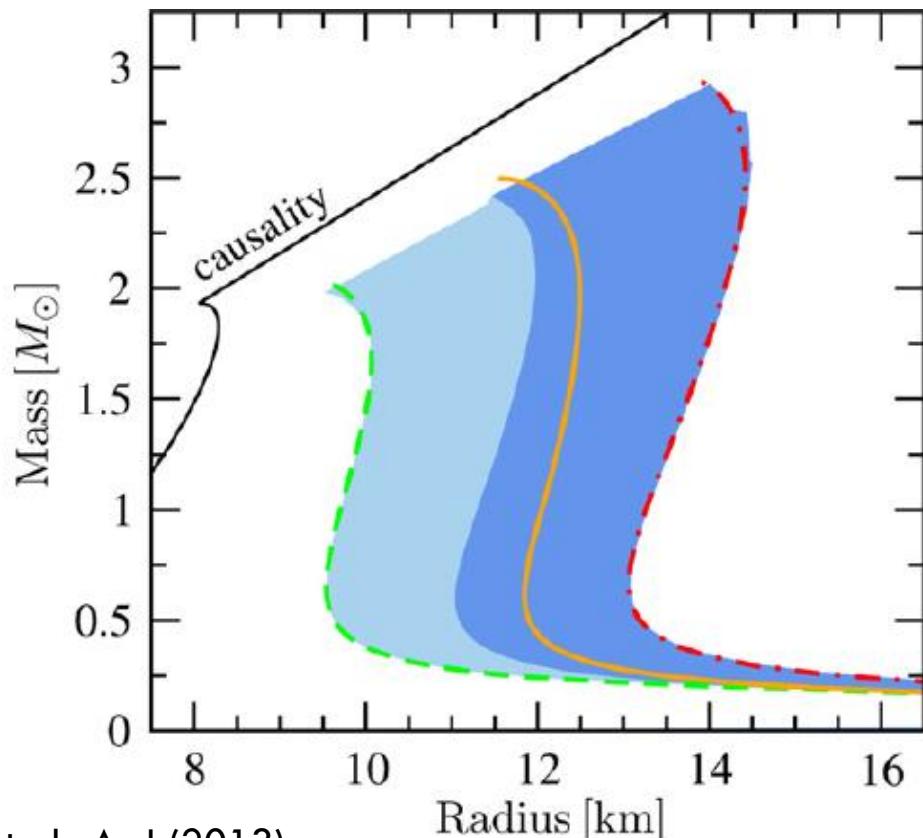
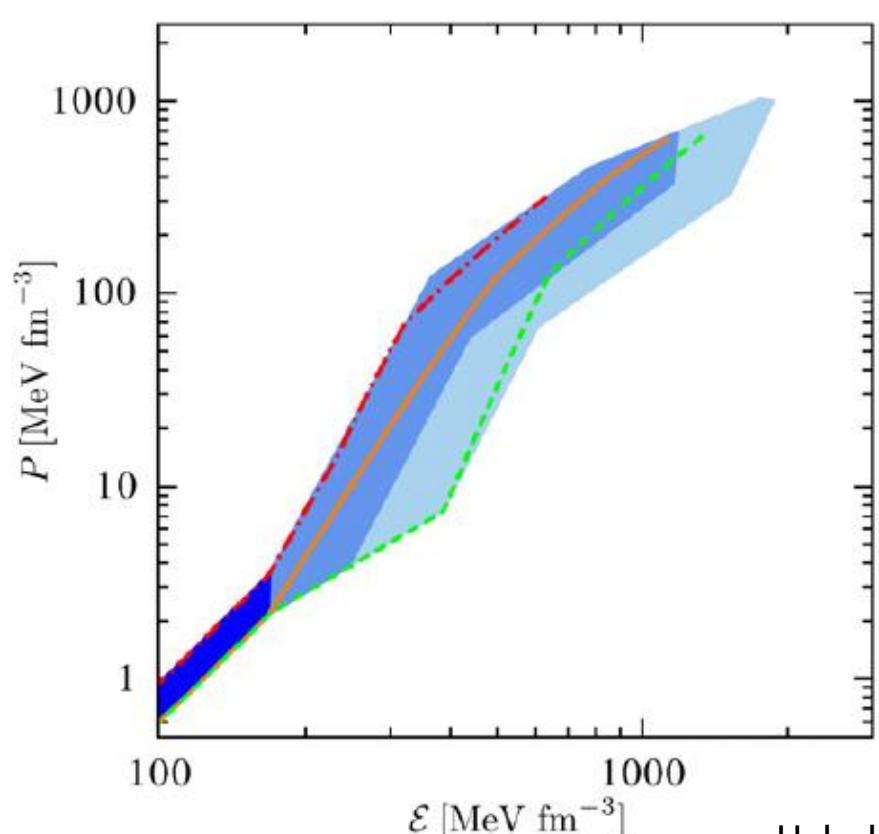
- Degenerate fluid of neutrons
- Non-strongly interacting neutrons
- Non-rotating

$$\rho_{\text{core}} \gtrsim \rho_{\text{nuc}} \sim 2.7 \times 10^{14} \text{ g/cm}^3$$

## Realistic Neutron Stars



# Constraining the nuclear EOS and Mass-Radius Relation



Hebeler et al., ApJ (2013)

# NS EOS (Relativistic Mean-Field-RMF- Models)

(Rueda, Ruffini, Xue, Nucl. Phys. A 872, 286, 2011)

$$\mathcal{L} = \mathcal{L}_g + \mathcal{L}_f + \mathcal{L}_\sigma + \mathcal{L}_\omega + \mathcal{L}_\rho + \mathcal{L}_\gamma + \mathcal{L}_{\text{int}}$$

$$\mathcal{L}_g = -\frac{R}{16\pi G},$$

$$\mathcal{L}_\gamma = -\frac{1}{16\pi} F_{\mu\nu} F^{\mu\nu},$$

$$\mathcal{L}_\sigma = \frac{1}{2} \nabla_\mu \sigma \nabla^\mu \sigma - U(\sigma), \quad U(\sigma) = U_0 + U(\sigma, 4)$$

$$\mathcal{L}_\omega = -\frac{1}{4} \Omega_{\mu\nu} \Omega^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu,$$

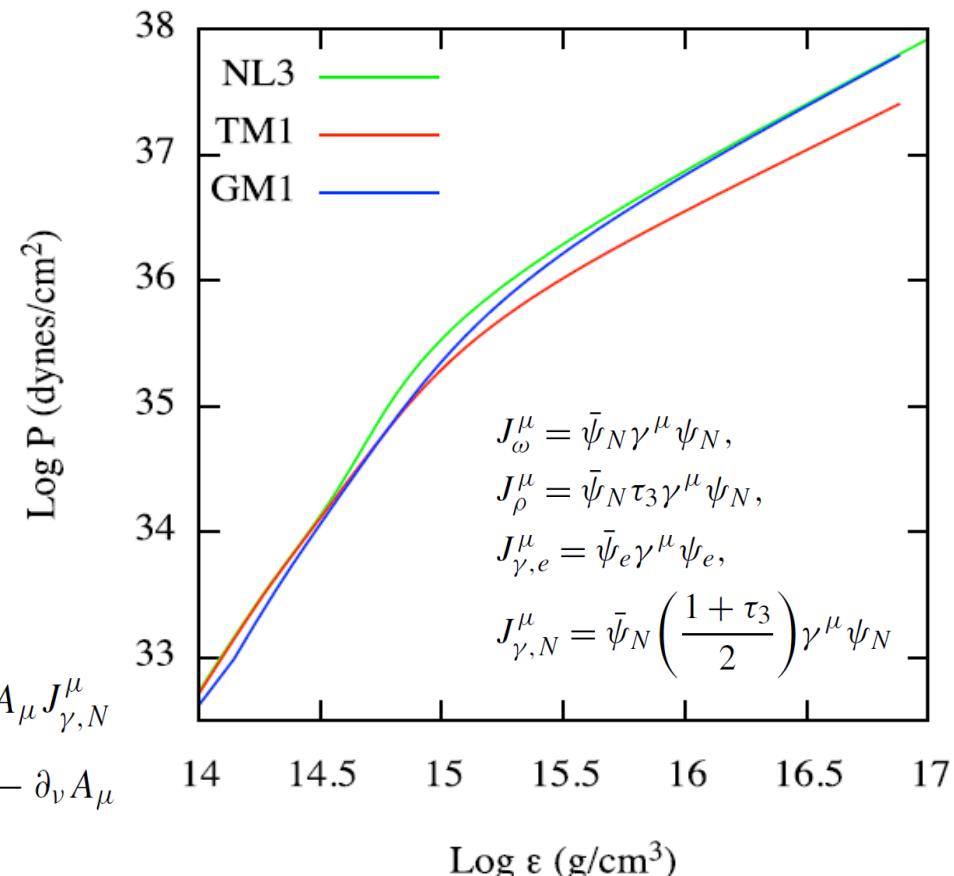
$$\mathcal{L}_\rho = -\frac{1}{4} \mathcal{R}_{\mu\nu} \mathcal{R}^{\mu\nu} + \frac{1}{2} m_\rho^2 \rho_\mu \rho^\mu,$$

$$\mathcal{L}_{\text{int}} = -g_\sigma \sigma \bar{\psi}_N \psi_N - g_\omega \omega_\mu J_\omega^\mu - g_\rho \rho_\mu J_\rho^\mu + e A_\mu J_{\gamma,e}^\mu - e A_\mu J_{\gamma,N}^\mu$$

$$\Omega_{\mu\nu} \equiv \partial_\mu \omega_\nu - \partial_\nu \omega_\mu, \quad \mathcal{R}_{\mu\nu} \equiv \partial_\mu \rho_\nu - \partial_\nu \rho_\mu, \quad F_{\mu\nu} \equiv \partial_\mu A_\nu - \partial_\nu A_\mu$$

$$U_0 \equiv \frac{1}{2} m_\sigma^2 \sigma^2,$$

$$U(\sigma, 4) \equiv \frac{1}{3} g_2 \sigma^3 + \frac{1}{4} g_3 \sigma^4$$



# Rotating NS configurations: full rotation in GR

(Cipolletta, Cherubini, Filippi, Rueda, Ruffini, PRD 92, 023007 (2015); arXiv: 1506.05926)

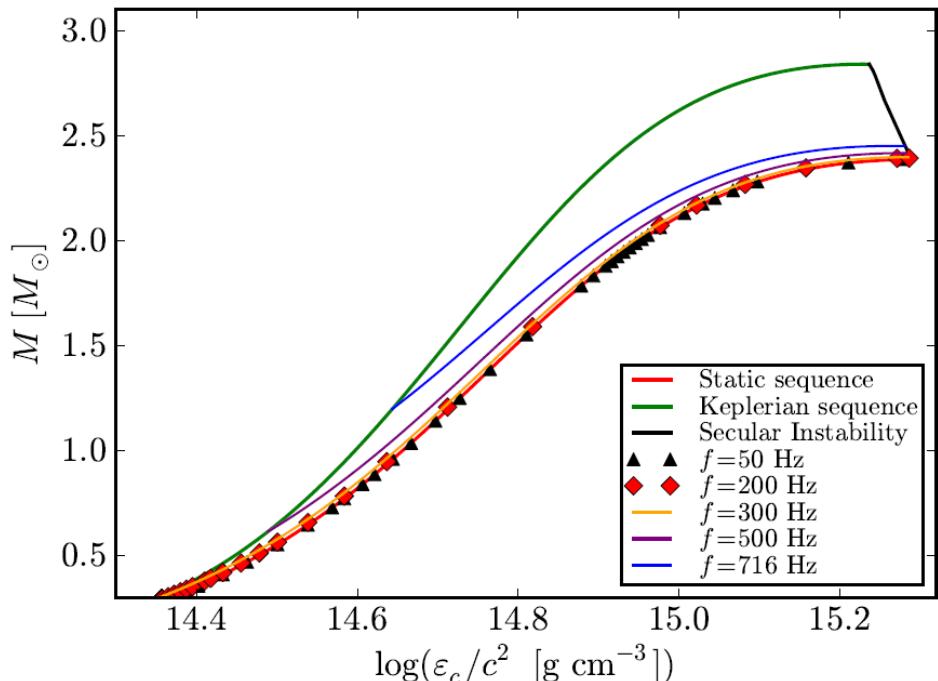
$$ds^2 = -e^{2\nu} dt^2 + e^{2\psi} (d\phi - \omega dt)^2 + e^{2\lambda} (dr^2 + r^2 d\theta^2) \quad T^{\alpha\beta} = (\varepsilon + P) u^\alpha u^\beta + Pg^{\alpha\beta}$$

$$\nabla \cdot (B \nabla \nu) = \frac{1}{2} r^2 \sin^2 \theta B^3 e^{-4\nu} \nabla \omega \cdot \nabla \omega + 4\pi B e^{2\zeta-2\nu} \left[ \frac{(\varepsilon + P)(1 + v^2)}{1 - v^2} + 2P \right]$$

$$\nabla \cdot (r^2 \sin^2 \theta B^3 e^{-4\nu} \nabla \omega) = -16\pi r \sin \theta B^2 e^{2\zeta-4\nu} \frac{(\varepsilon + P)v}{1 - v^2} \quad \nabla \cdot (r \sin(\theta) \nabla B) = 16\pi r \sin \theta B e^{2\zeta-2\nu} P,$$

$$\begin{aligned} \zeta_{,\mu} = & - \left\{ (1 - \mu^2) \left( 1 + r \frac{B_{,r}}{B} \right)^2 + \left[ \mu - (1 - \mu^2) \frac{B_{,r}}{B} \right]^2 \right\}^{-1} \left[ \frac{1}{2} B^{-1} \left\{ r^2 B_{,rr} - [(1 - \mu^2) B_{,\mu}]_{,\mu} - 2\mu B_{,\mu} \right\} \right. \\ & \times \left\{ -\mu + (1 - \mu^2) \frac{B_{,\mu}}{B} \right\} + r \frac{B_{,r}}{B} \left[ \frac{1}{2} \mu + \mu r \frac{B_{,r}}{B} + \frac{1}{2} (1 - \mu^2) \frac{B_{,\mu}}{B} \right] + \frac{3}{2} \frac{B_{,\mu}}{B} \left[ -\mu^2 + \mu (1 - \mu^2) \frac{B_{,\mu}}{B} \right] \\ & - (1 - \mu^2) r \frac{B_{,\mu r}}{B} \left( 1 + r \frac{B_{,r}}{B} \right) - \mu r^2 (\nu_{,r})^2 - 2 (1 - \mu^2) r \nu_{,\mu} \nu_{,r} + \mu (1 - \mu^2) (\nu_{,\mu})^2 - 2 (1 - \mu^2) r^2 B^{-1} B_{,r} \nu_{,\mu} \nu_{,r} \\ & + (1 - \mu^2) B^{-1} B_{,\mu} \left[ r^2 (\nu_{,r})^2 - (1 - \mu^2) (\nu_{,\mu})^2 \right] + (1 - \mu^2) B^2 e^{-4\nu} \left\{ \frac{1}{4} \mu r^4 (\omega_{,r})^2 + \frac{1}{2} (1 - \mu^2) r^3 \omega_{,\mu} \omega_{,r} \right. \\ & \left. - \frac{1}{4} \mu (1 - \mu^2) r^2 (\omega_{,\mu})^2 + \frac{1}{2} (1 - \mu^2) r^4 B^{-1} B_{,r} \omega_{,\mu} \omega_{,r} - \frac{1}{4} (1 - \mu^2) r^2 B^{-1} B_{,\mu} \left[ r^2 (\omega_{,r})^2 - (\mu^2) (\omega_{,\mu})^2 \right] \right\} \end{aligned}$$

# Rotating NS configurations: secular instability line

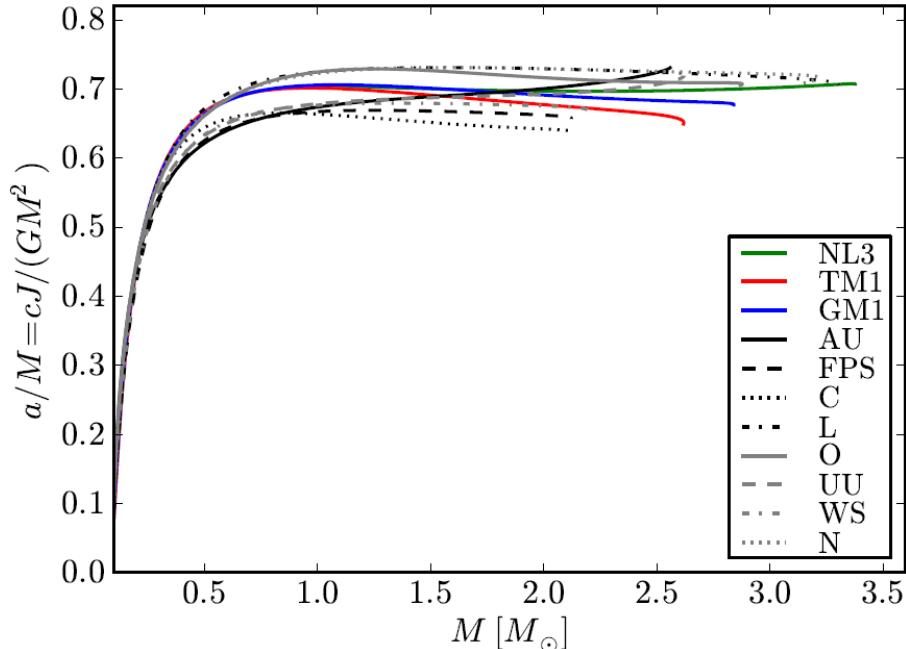
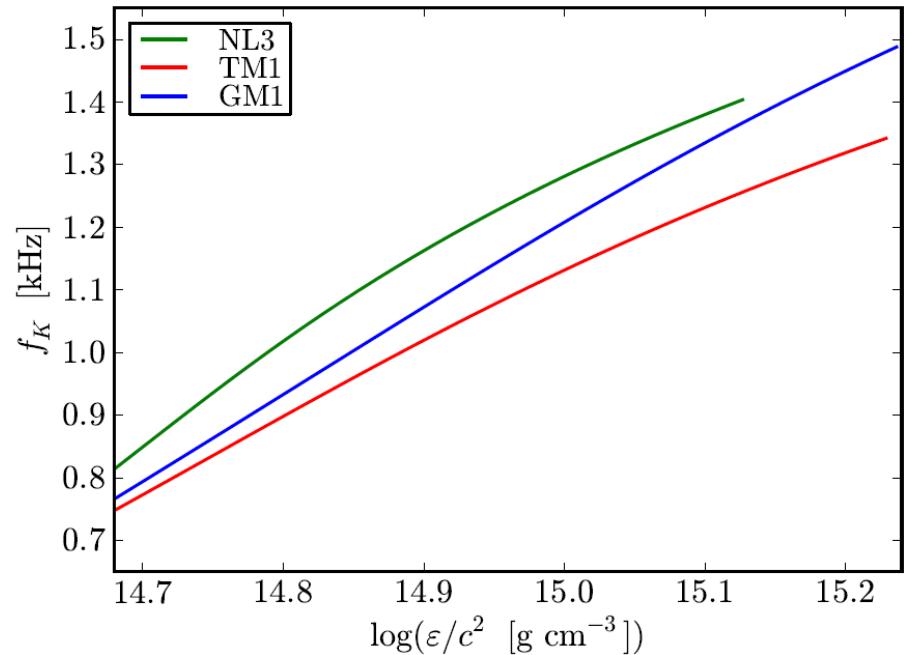


$$M_{\text{NS}}^{\text{crit}} = M_{\text{NS}}^{J=0} (1 + k j_{\text{NS}}^p)$$

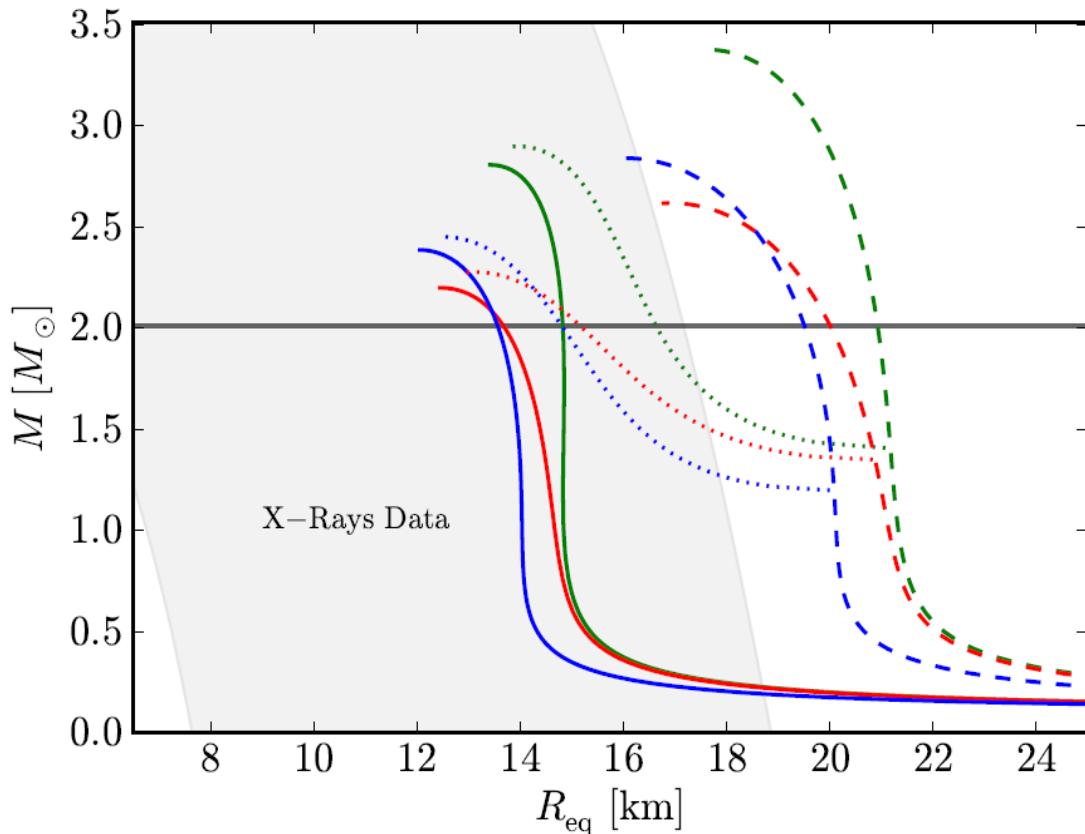
	$M_{\text{crit}}^{J=0}$ $M_{\odot}$	$R_{\text{crit}}^{J=0}$ km	$M_{\max}^{J \neq 0}$ $M_{\odot}$	$R_{\max}^{J \neq 0}$ km	$f_K$ kHz	$p$	$k$
NL3	2.81	13.49	3.38	17.35	1.34	1.68	0.006
GM1	2.39	12.56	2.84	16.12	1.49	1.69	0.011
TM1	2.20	12.07	2.62	15.98	1.40	1.61	0.017

Taken from Cipolletta, et al. PRD 92, 023007 (2015)  
arXiv: 1506.05926

# Rotating NS configurations: full rotation in GR



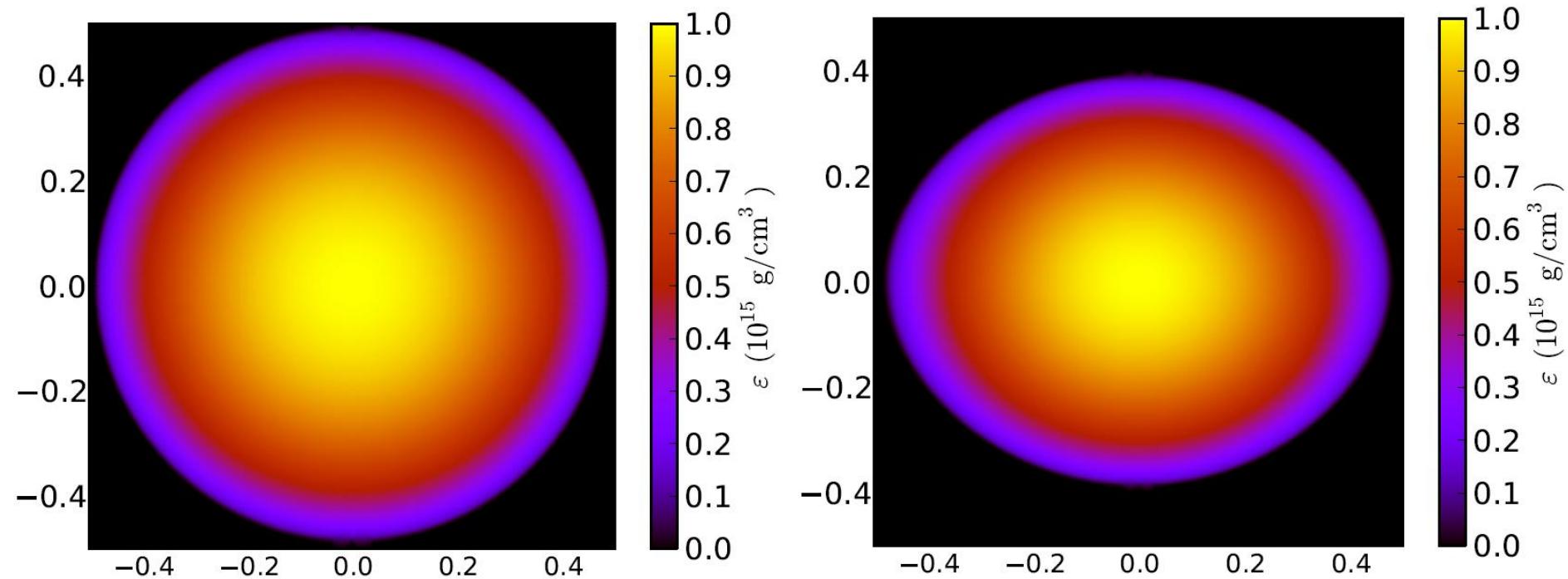
# NS Mass-Radius Relation: Observational Constraints



- Maximum NS mass observed:  
 $2 M_{\odot}$   
(Antoniadis et al., Science (2013))
- Fastest NS observed:  $f=716 \text{ Hz}$   
(Demorest et al., Science (2006))
- Radii from X-ray emission: mainly  
from low-mass X-ray binaries  
(LMXBs), and X-ray isolated NSs  
(XINSs): shaded area  
(Lattimer & Steiner, EPJ (2014))

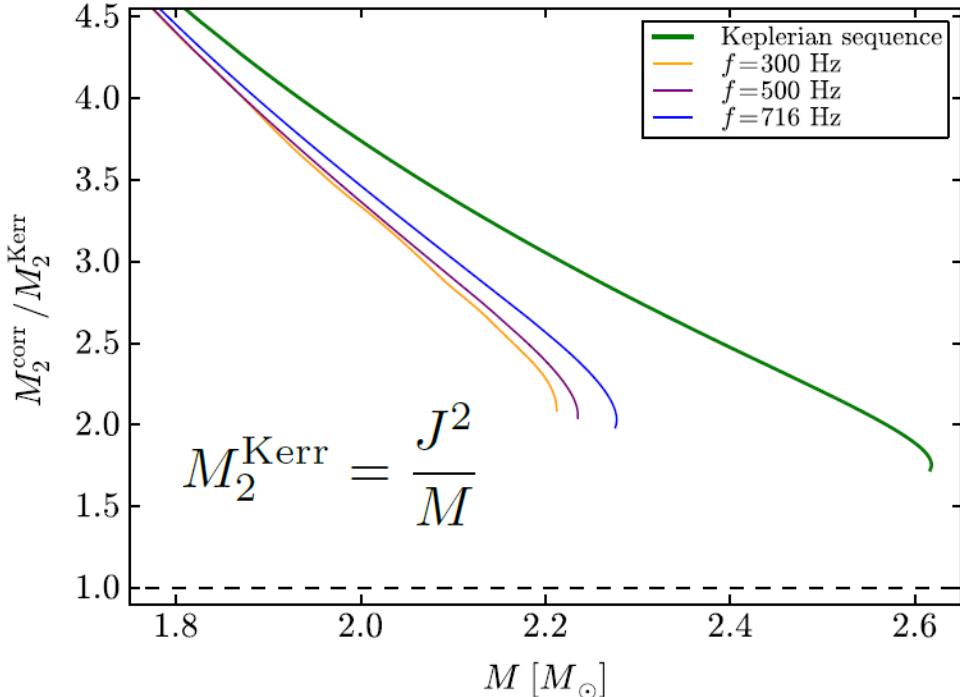
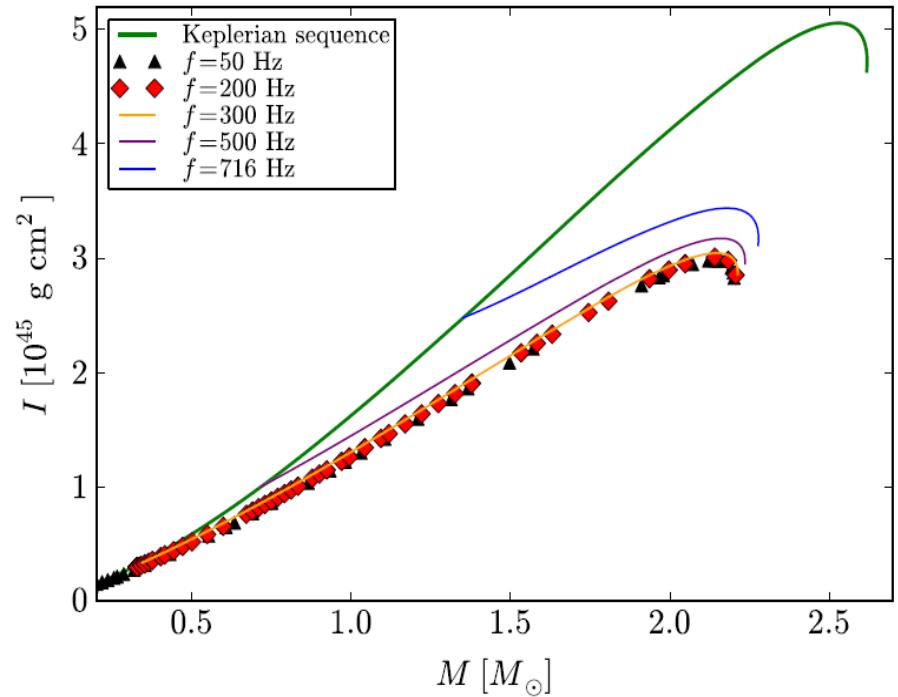
# Rotating NS: Deformation

(Cipolletta, Cherubini, Filippi, Rueda, Ruffini, PRD 92, 023007 (2015); arXiv: 1506.05926)



# NS moment of inertia and quadrupole moment

(Cipolletta, Cherubini, Filippi, Rueda, Ruffini, PRD 92, 023007 (2015); arXiv: 1506.05926)



# Neutron Star Binding Energy

(Cipolletta, Cherubini, Filippi, Rueda, Ruffini, PRD 2015; arXiv: 1506.05926)

Static Configurations

$$\frac{M_b}{M_\odot} \approx \frac{M}{M_\odot} + \frac{13}{200} \left( \frac{M}{M_\odot} \right)^2$$

$c \text{ J}/(\text{G } M_\odot^2)$

Rotating Configurations

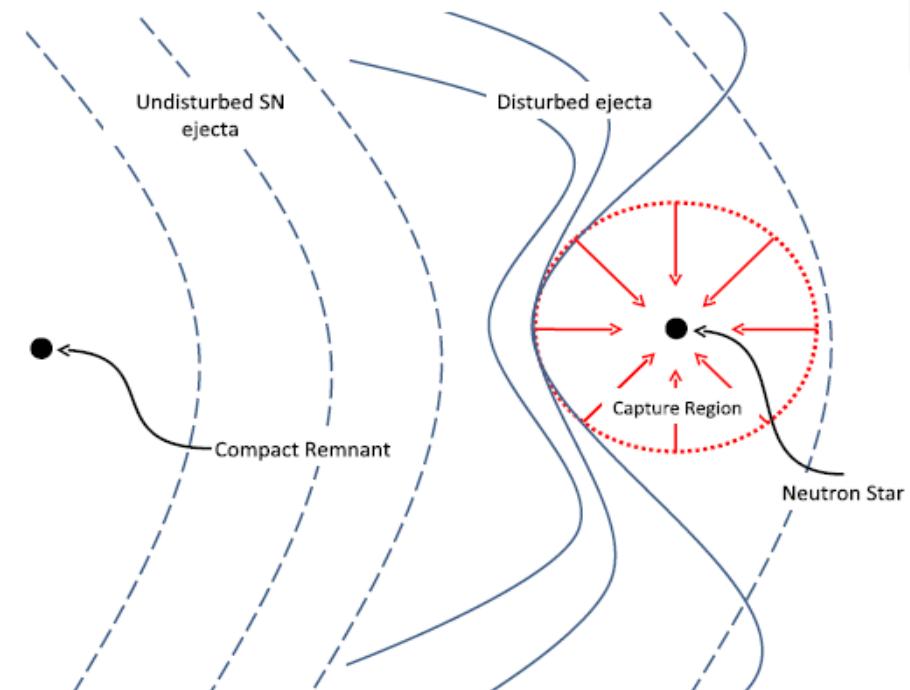
$$\frac{M_b}{M_\odot} = \frac{M}{M_\odot} + \frac{13}{200} \left( \frac{M}{M_\odot} \right)^2 \left( 1 - \frac{1}{130} j^{1.7} \right)$$

# First estimates of the accretion process

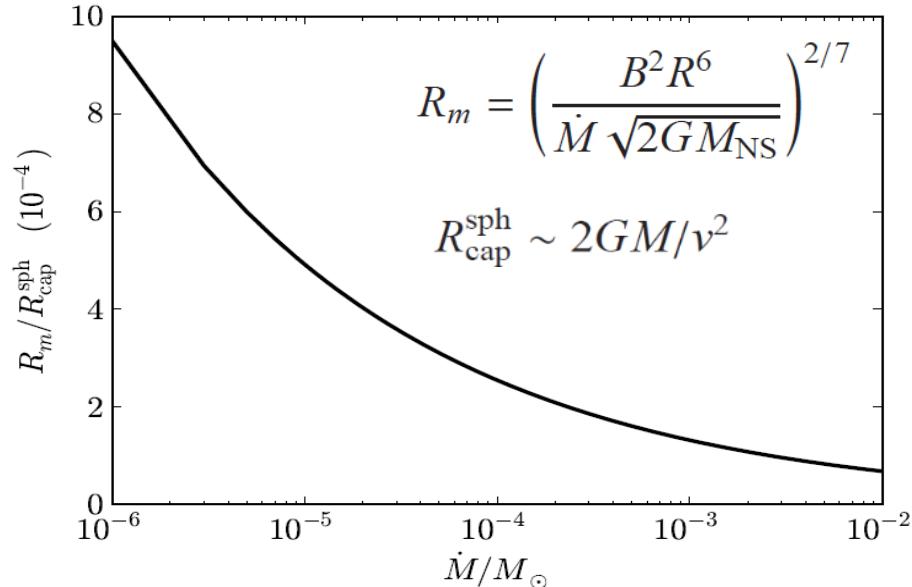
Rueda & Ruffini, ApJ Lett. 758, L7 (2012)

Izzo, Rueda, Ruffini, A&A Lett. 548, L5 (2012)

$$R_{\text{cap}} = \frac{2GM_{\text{NS}}}{v_{\text{rel,ej}}^2}, \quad v_{\text{rel,ej}} = \sqrt{v_{\text{orb}}^2 + v_{\text{ej}}^2}, \quad r_{\text{ej}} = \sigma t^n$$



## The relative importance of the magnetosphere



See also Toropina, Romanova, Lovelace, MNRAS 420, 810 (2012)

**How long is the accretion process?  
Does the neutron star reach maximum mass?**

**Which is the initial mass of the  
neutron star?**

**Which is the maximum stable  
mass of a neutron star?**

# Improvements to the First IGC Scenario

- **SN core density and SN initial velocity profiles from numerical simulations**
- **SN core and NS masses from binary evolution codes**
- **Hydrodynamics inside the Bondi accretion region: photon trapping radius, neutrino emission**
- **Characteristic emission from the accretion process**
  - ...

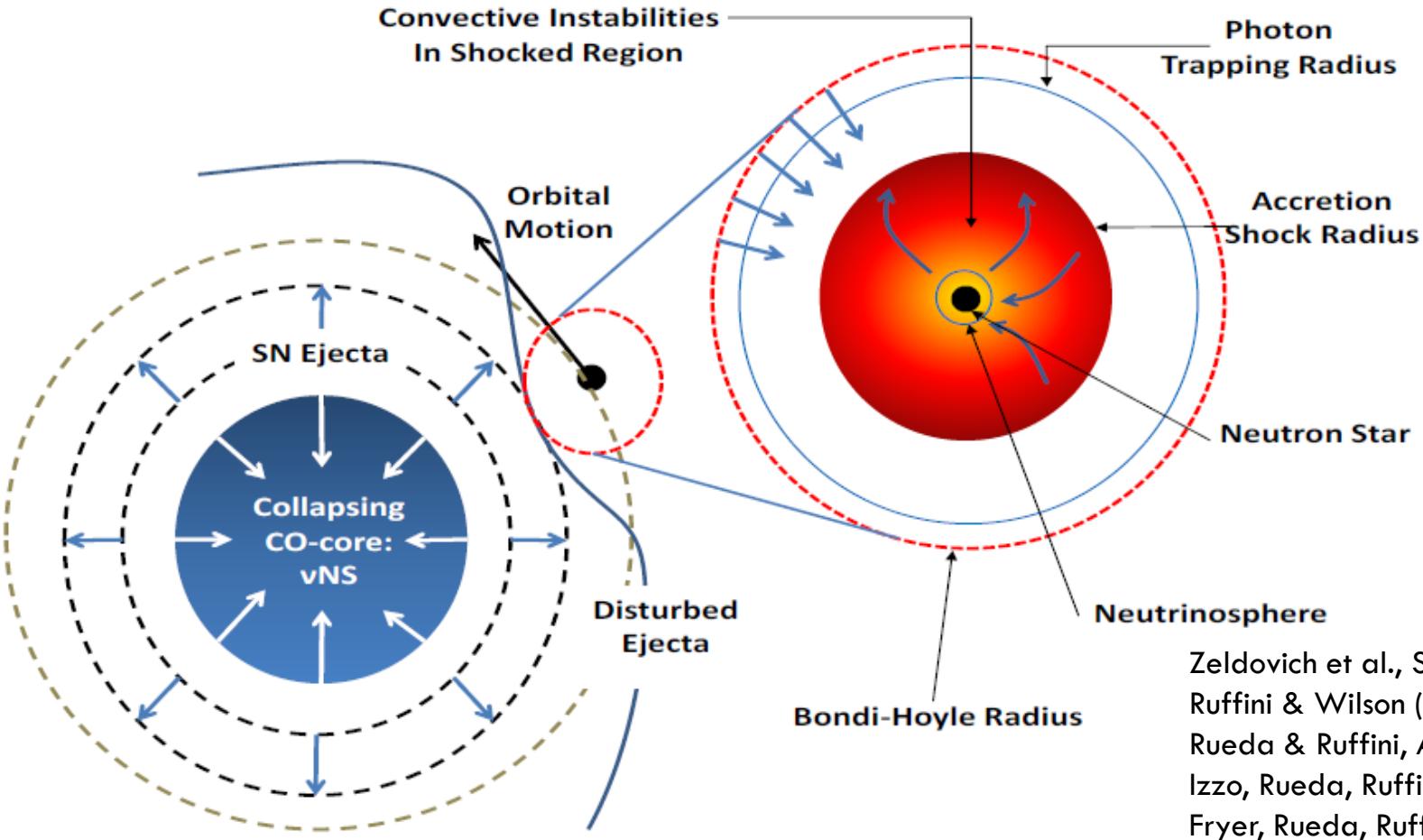
# Hypercritical Accretion

## Conditions for Eddington limited accretion:

- Potential energy is released in the form of photons
- Inflowing material and outflowing radiation are spherically symmetric
- Photons can flow and deposit momentum to the inflowing material
  - Opacity is dominated by electron scattering

***NONE OF THE ABOVE CONDITIONS IS SATISFIED IN THE  
IGC BINARY SYSTEM !!!***

# Binary Driven Hypercritical Accretion in the IGC

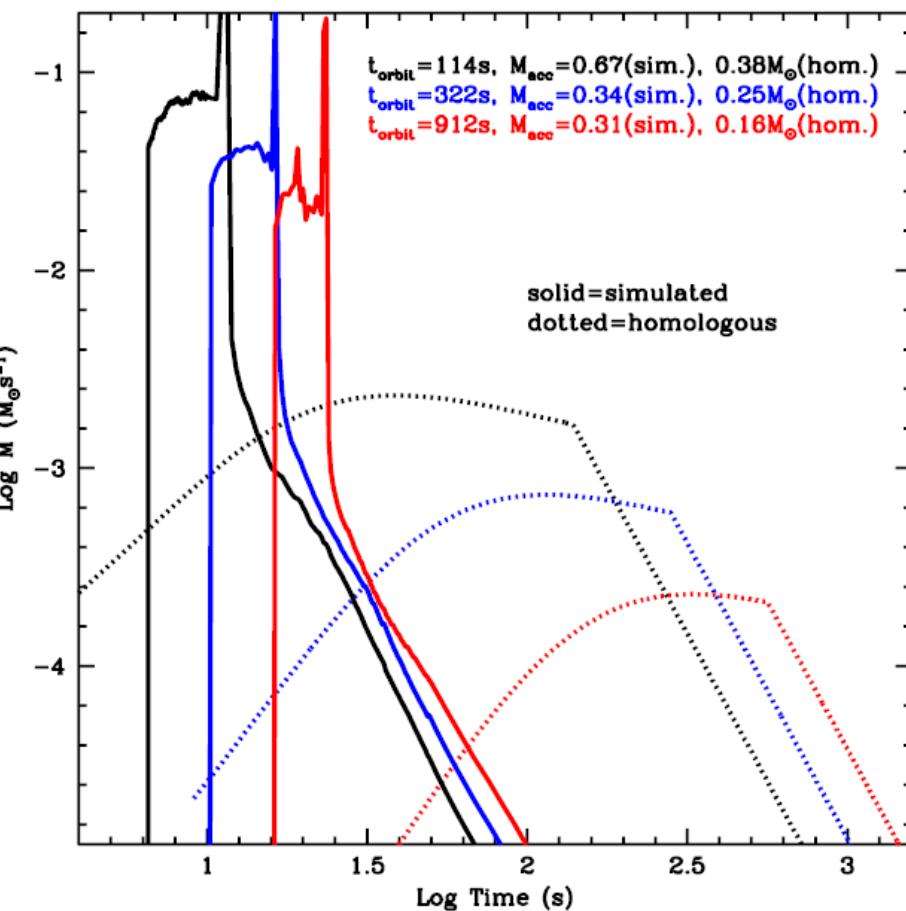
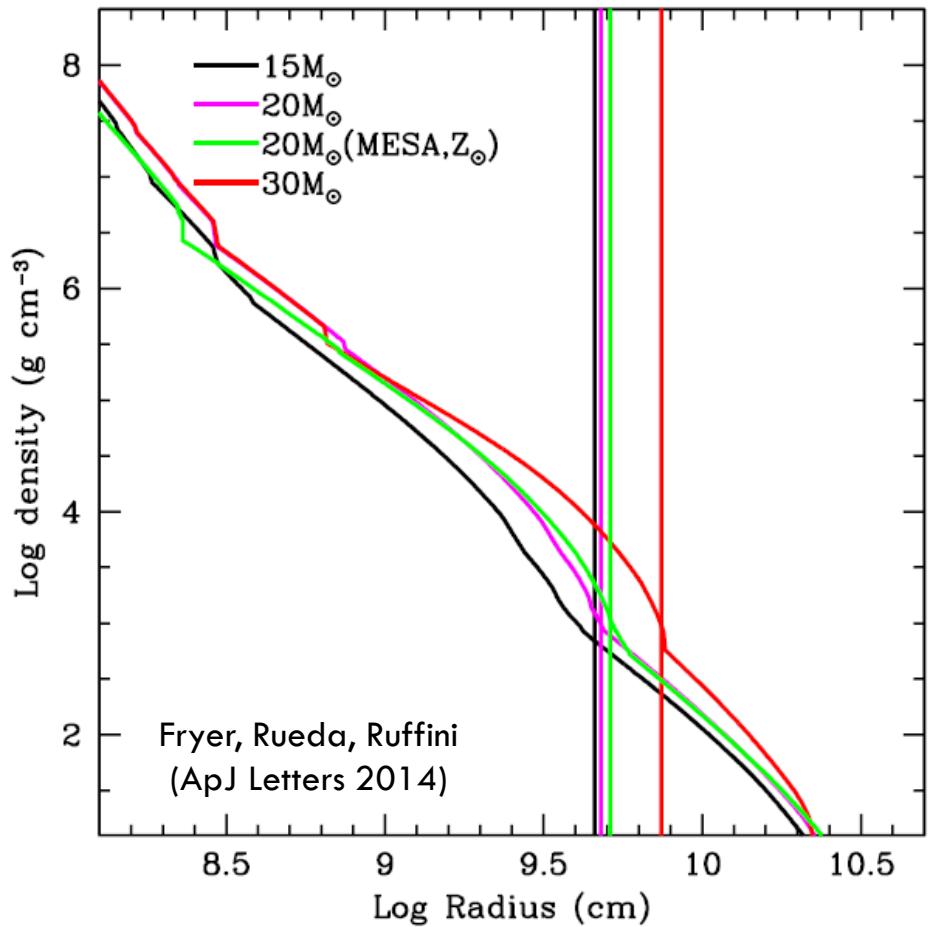


Zeldovich et al., Sov. Astron. (1972)  
Ruffini & Wilson (1973)  
Rueda & Ruffini, ApJL (2012)  
Izzo, Rueda, Ruffini, A&AL (2012)  
Fryer, Rueda, Ruffini, ApJL (2014)

$$\dot{M}_{\text{BHL}} = 4\pi r_{\text{BHL}}^2 \rho (v^2 + c_s^2)^{1/2}$$

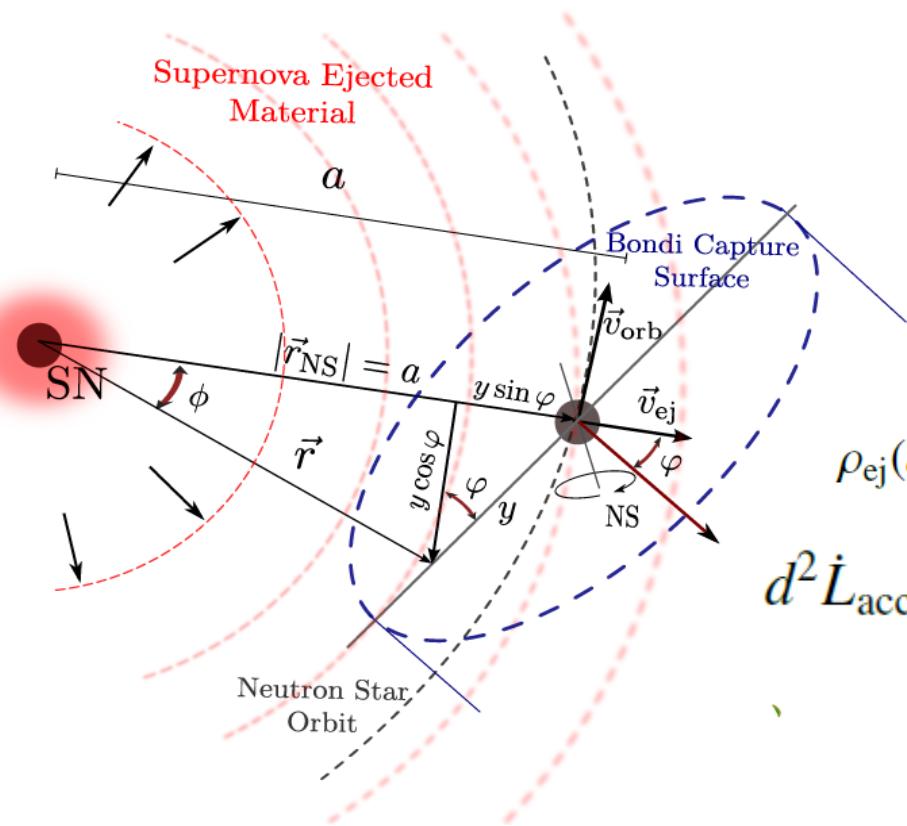
$$r_{\text{BHL}} = \frac{GM_{\text{NS}}}{v^2 + c_s^2}$$

$$r_{\text{trapping}} = \min[(\dot{M}_{\text{BHL}} \kappa) / (4\pi c), r_{\text{BHL}}]$$



# On the role of angular momentum in BdHNe

(Becerra, Cipolletta, Fryer, Rueda, Ruffini, ApJ 2015; arXiv: 1505.07580 )



$$\dot{M}_B(t) = \pi \rho_{ej} R_{cap}^2 \sqrt{v_{rel}^2 + c_{s,ej}^2}$$

$$R_{cap}(t) = \frac{2GM_{NS}(t)}{v_{rel}^2 + c_{s,ej}^2}$$

$$\rho_{ej}(a) \simeq \rho_{ej}(a)(1 + \epsilon_\rho y) \quad \text{and} \quad v_{rel}(a) \simeq v_{rel}(a)(1 + \epsilon_v y)$$

$$d^2\dot{L}_{acc} = \rho_{ej}(a)v_{rel}^2(a) \left[ y + (\epsilon_\rho + 2\epsilon_v)y^2 \right] dy dz$$

$$y^2 + z^2 = R_{cap}^2 = \left( \frac{2GM_{NS}}{v_{rel}^2(a,t)} \right)^2 (1 - 4\epsilon_v y)$$

# On the role of angular momentum in BdHNe

(Becerra, Cipolletta, Fryer, Rueda, Ruffini, ApJ 2015; arXiv:1505.07580)

$$\dot{L}_{\text{acc}} = \frac{\pi}{2} \left( \frac{1}{2} \epsilon_p - 3 \epsilon_v \right) \rho_{\text{ej}}(a, t) v_{\text{rel}}^2(a, t) R_{\text{cap}}^4(a, t)$$

$$\rho_{\text{ej}}(x, t) = \rho_{\text{ej}}(x, t_0) \frac{M_{\text{env}}(t)}{M_{\text{env}}(t_0)} \left( \frac{R_{0\text{star}}}{R_{\text{star}}(t)} \right)^3 \quad x \equiv \frac{r}{R_{\text{star}}}$$

$$R_{\text{star}}(t) = R_{0\text{star}} \left( \frac{t}{t_0} \right)^n \quad v_{\text{ej}}(r, t) = n \frac{r}{t}$$

$$\rho_{\text{ej}}(r, t) \approx \rho_{\text{ej}}(a, t) \left( 1 + \frac{1}{\rho_{\text{ej}}(a, t)} \left. \frac{\partial \rho_{\text{ej}}}{\partial r} \right|_{(a,t)} \delta r \right)$$

$$v_{\text{ej}}(r, t) \approx v_{\text{ej}}(a, t) \left( 1 + \frac{1}{v_{\text{ej}}(a, t)} \left. \frac{\partial v_{\text{ej}}}{\partial r} \right|_{(a,t)} \delta r \right)$$

$$\dot{L}_{\text{acc}} = 8\pi \rho_{\text{core}} \left( \frac{R_{\text{core}}}{a} \right)^m \frac{GM_{\text{NS}}(t_0)a^2}{(1+q)^3} H(y)$$

$$H(y) = y^{n(m-3)} \left( \frac{M_{\text{G}}(M_b)}{M_{\text{NS}}(t_0)} \right)^4 (1-\chi\mu_B) \left( 1 + \frac{\eta}{y^2} \right)^{-7/2} \left( \frac{m}{2} + \frac{6\eta}{y^2 + \eta} \right)$$

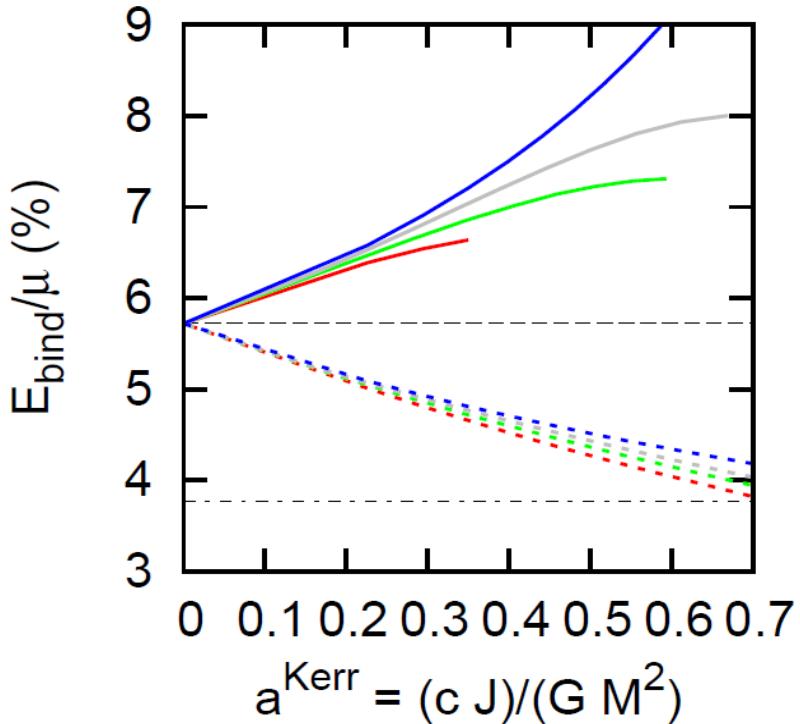
$$\frac{\dot{\mu}_B}{(1-\chi\mu_B)M_{\text{G}}(M_b)^2} = \frac{t_0}{\tau_B} \frac{y^{n(m-3)}}{\hat{r}^m} \left[ 1 + \eta \left( \frac{\hat{r}}{y} \right)^2 \right]^{-3/2}$$

$$y \equiv \frac{t}{t_0}, \quad \mu_B \equiv \frac{M_B(y)}{M_{\text{NS}}(t_0)}, \quad \hat{r} \equiv 1 - \frac{R_B}{a}$$

$$\tau_B \equiv \frac{M_{\text{NS}}(t_0)v_{\text{orb}}^3}{4\pi G^2 \rho_{\text{ej}}(a, t_0)}, \quad \chi \equiv \frac{M_{0\text{NS}}}{M_{\text{env}}(t_0)}, \quad \eta \equiv \left( \frac{n}{t_0} \frac{a}{v_{\text{orb}}} \right)^2$$

# Mostly bound circular orbit around rotating NSs

(Cipolletta, Rueda, Ruffini, PRD, submitted)



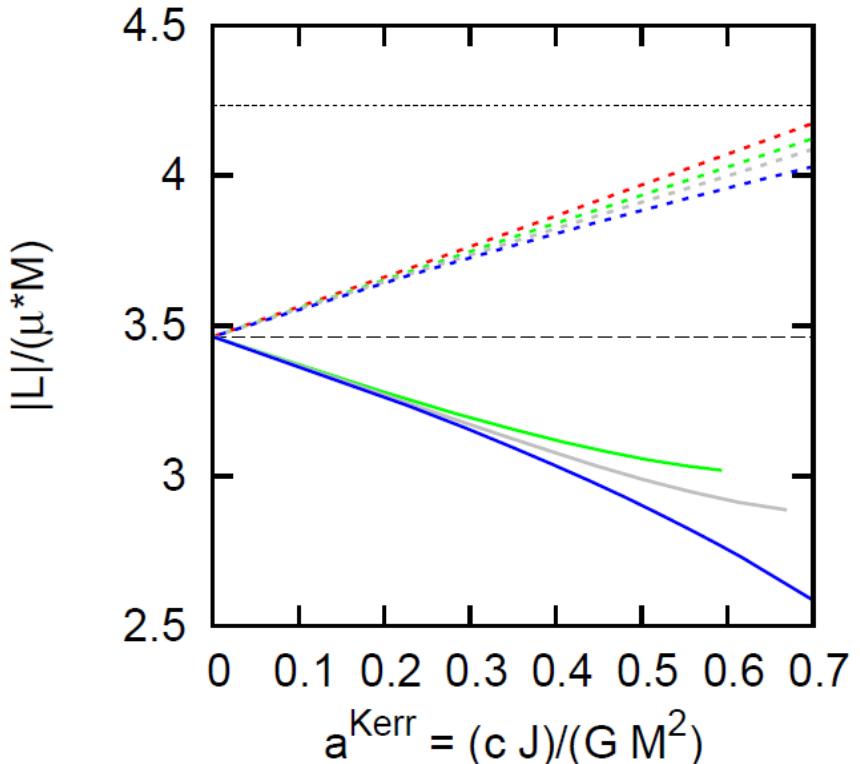
Schw = 5.72 %  
Ex Kerr - = 3.77 %  
 $E_+$  for  $M = 2$   
 $E_-$  for  $M = 2$   
 $E_+$  for  $M = 2.4$   
 $E_-$  for  $M = 2.4$   
 $E_+$  for  $M = 2.8$   
 $E_-$  for  $M = 2.8$   
 $E_+$  Kerr  
 $E_-$  Kerr

Numerical Fit (common for the RMF EOS !):

$$\tilde{E} = 0.9428 - 0.0132 \left( \frac{j}{M} \right)^{0.85}$$

# Mostly bound circular orbit around rotating NSs

(Cipolletta, Rueda, Ruffini, PRD, submitted)



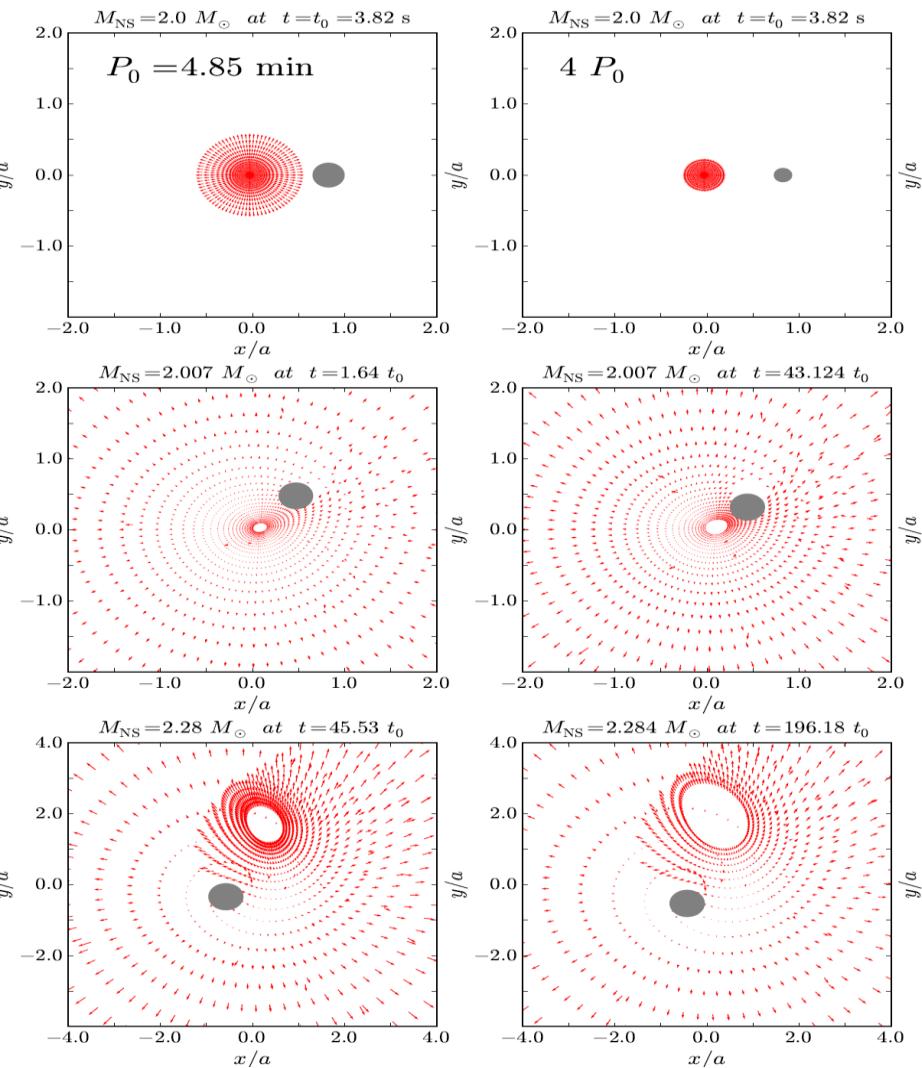
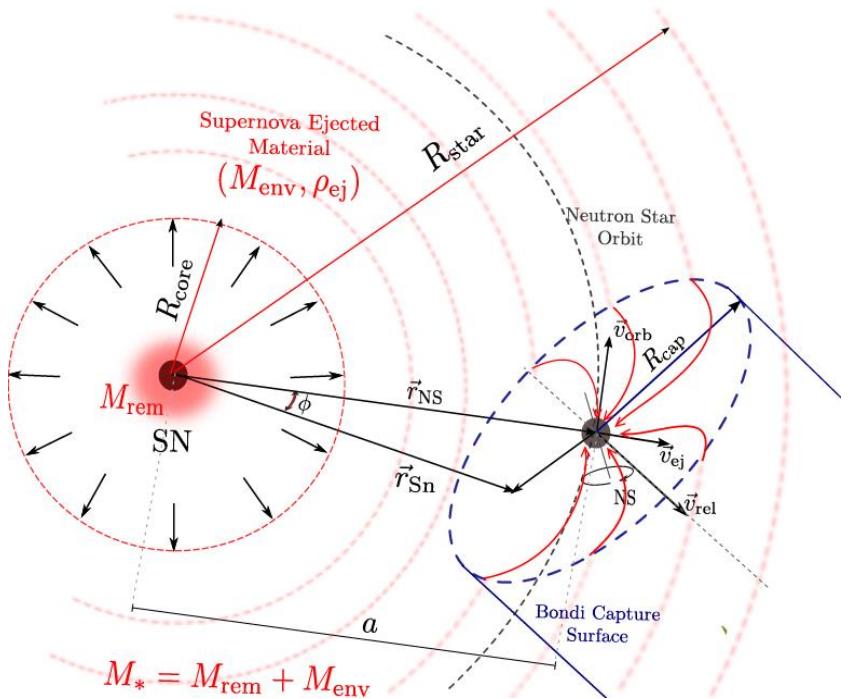
- |       |                            |       |
|-------|----------------------------|-------|
| $L_+$ | Schw = $2\sqrt{3}$         | ---   |
| $L_-$ | ex Kerr = $22/(3\sqrt{3})$ | ----- |
| $L_+$ | for $M = 2$                | - - - |
| $L_-$ | for $M = 2$                | - - - |
| $L_+$ | for $M = 2.4$              | - - - |
| $L_-$ | for $M = 2.4$              | - - - |
| $L_+$ | for $M = 2.8$              | - - - |
| $L_-$ | for $M = 2.8$              | - - - |
| $L_+$ | Kerr                       | - - - |
| $L_-$ | Kerr                       | - - - |

Numerical Fit (common for the RMF EOS !):

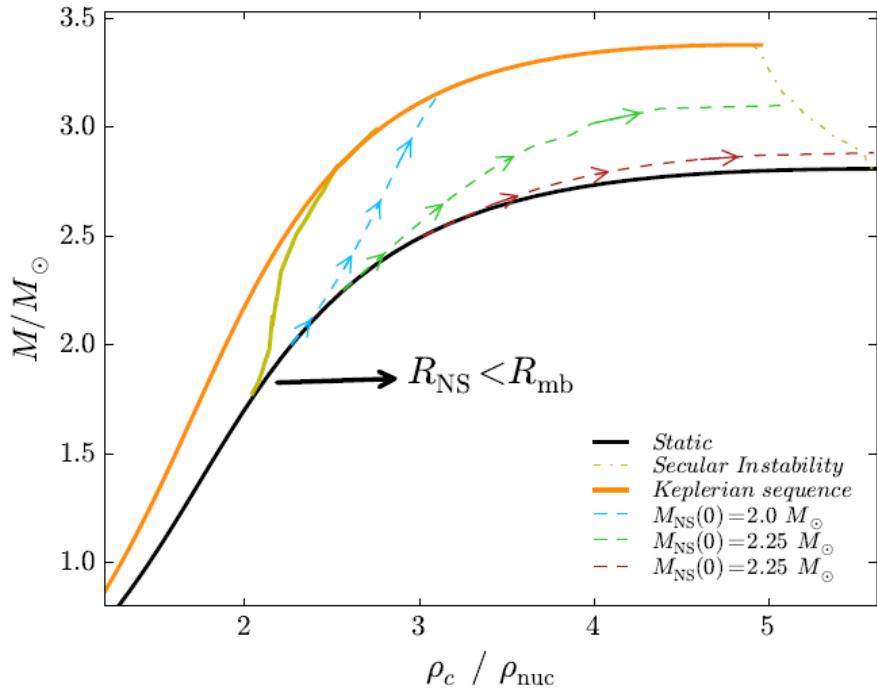
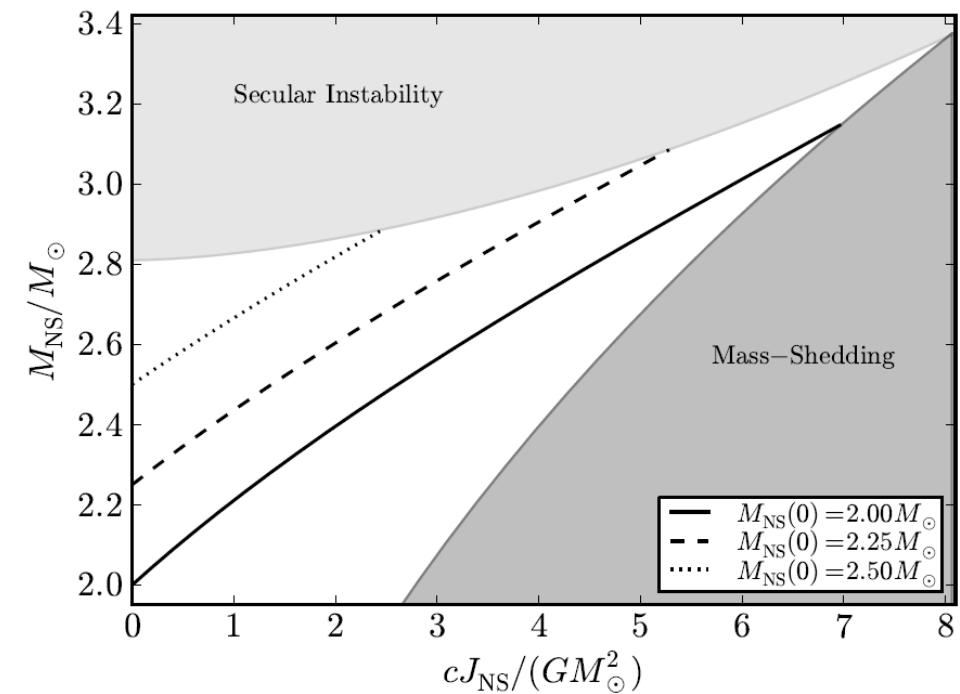
$$\tilde{L} = 3.464 - 0.37 \left( \frac{j}{M} \right)^{0.85}$$

# NS evolution during hypercritical accretion

Becerra, Cipolletta, Fryer, Rueda, Ruffini, ApJ 2015:  
arXiv:1505.07580

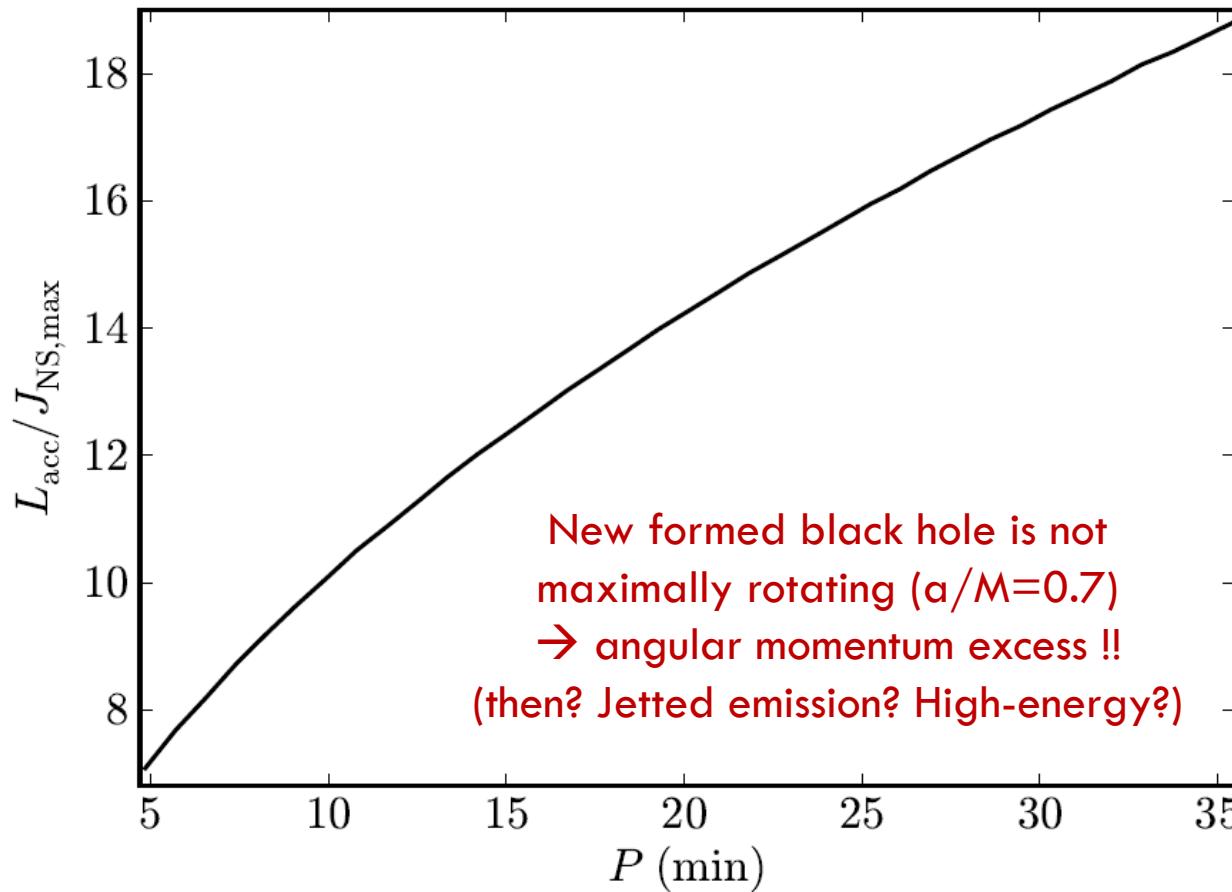


# NS evolution up to the instability point



# On the role of angular momentum in BdHNe

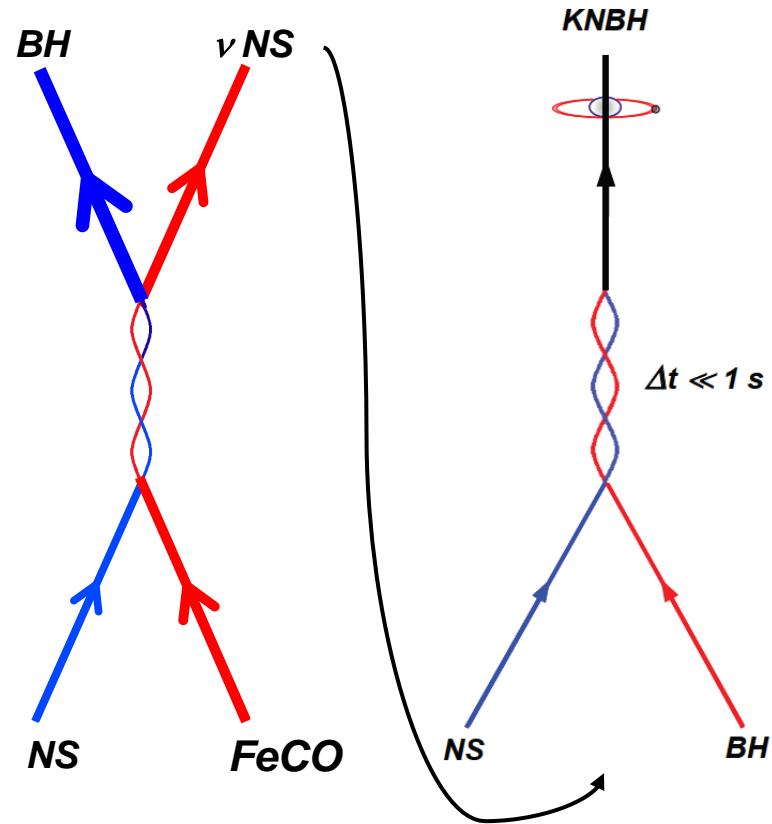
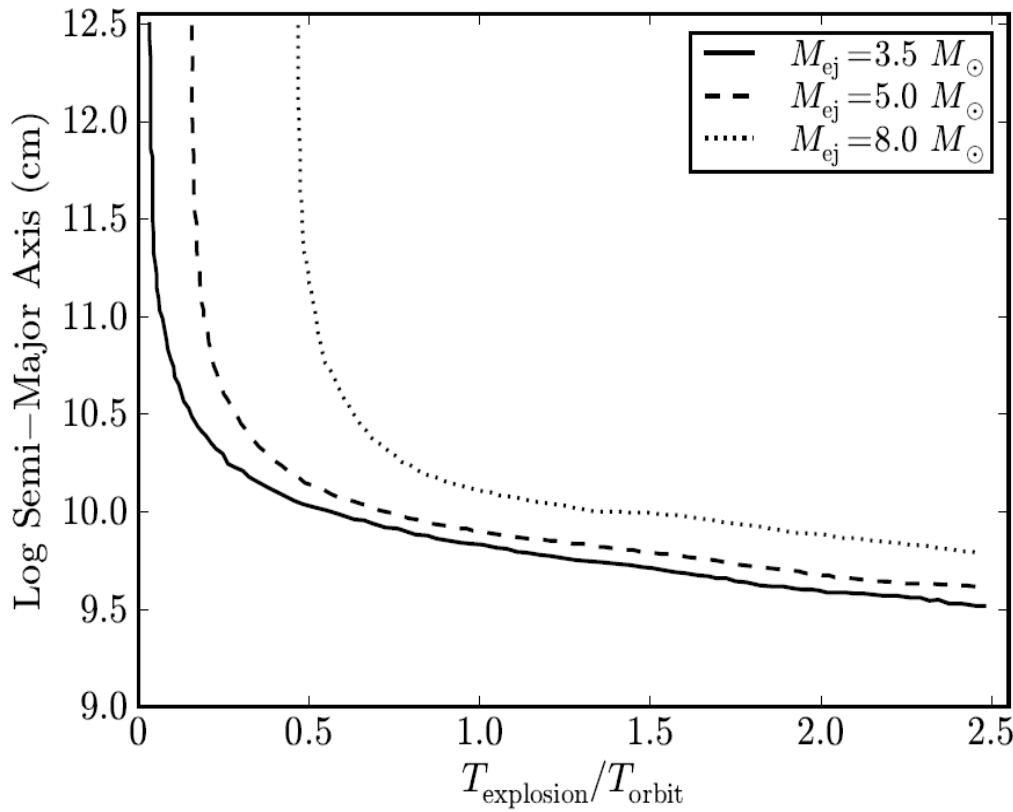
(Becerra, Cipolletta, Fryer, Rueda, Ruffini, ApJ 2015; arXiv: 1505.07580 )



# What's next?

## On the NS-BH binaries produced by BdHNe

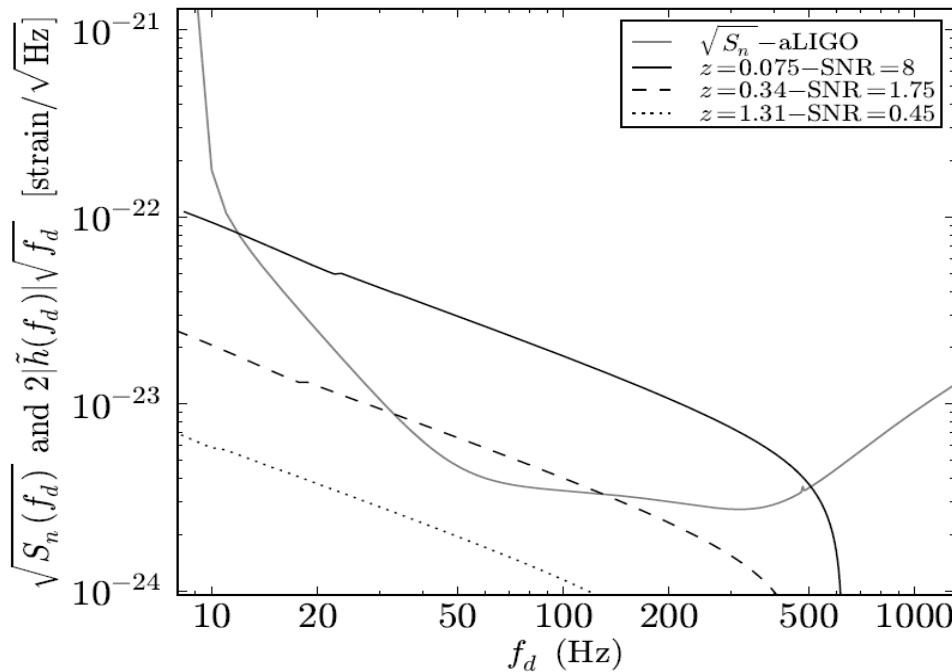
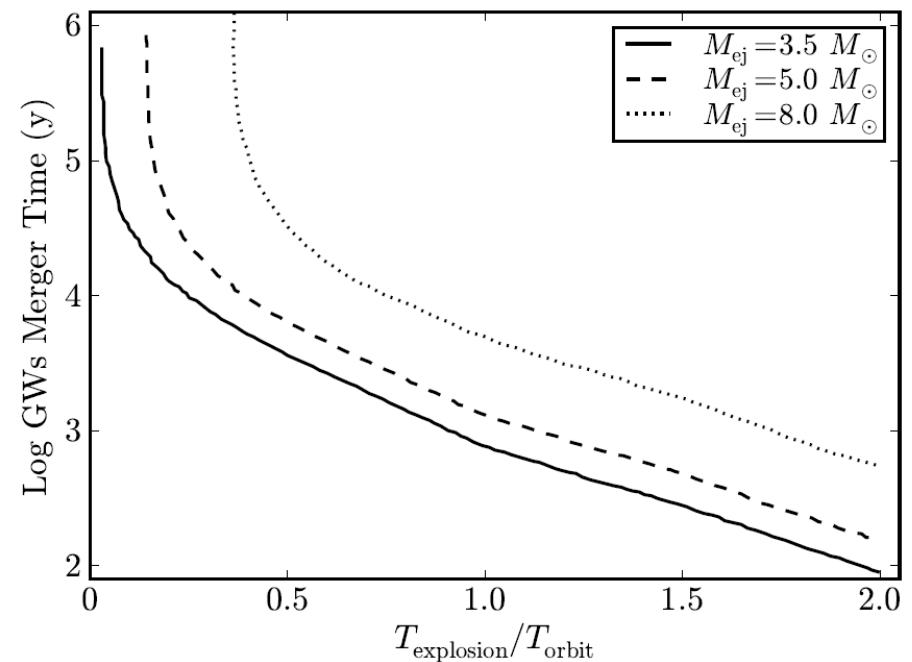
(Fryer, Oliveira, Rueda, Ruffini, Phys. Rev. Lett., in press)



# What's next?

## On the NS-BH binaries produced by BdHNe

(Fryer, Oliveira, Rueda, Ruffini, Phys. Rev. Lett., in press)



# CONCLUSION

